

$\hat{\mu}$   $p < 0.01$   $N$   
 $\hat{\sigma}/\sqrt{n}$  n.s.  $x_i^2$   
 5% sig.  $\mu$   $s = \frac{\sum(x_i - \mu)^2}{n-1}$

## Understanding Statistics for HCI and Related Disciplines

### Part 3 – Gaining Power

#### the dreaded ‘too few participants’

Alan Dix  
<http://alandix.com/statistics/>

$$P(A | B) = \frac{P(A) \cdot P(B|A)}{P(B)}$$

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### don't you hate it when ...

=== Reviewer 2

Although the premise seems sound there are too few participants to be able to draw meaningful conclusions.

=== Reviewer 3

P= 0.673 not significant

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### statistical power – what is it?

if there is a real effect  
 how likely are you to be able to detect it?

avoiding false negatives

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### increasing power


standard approach ...  
 add more participants

but not the only way!

can get more power ...  
 but often sacrifice a little generality  
 need to understand and explain

with great power comes great responsibility ;-)

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### noise–effect–number triangle

three routes to gain power

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## recall Stats 101 (for simple data)

$\sigma$  – standard deviation of data

often 'noise' – things you can't control or measure  
e.g. individual variability

s.e. – standard error of mean (s.e.)

the accuracy of your estimate (error bars)

s.e. =  $\sigma / \sqrt{n}$  (if  $\sigma$  is an estimate  $\sqrt{n-1}$ )  
to half standard error you must quadruple number.

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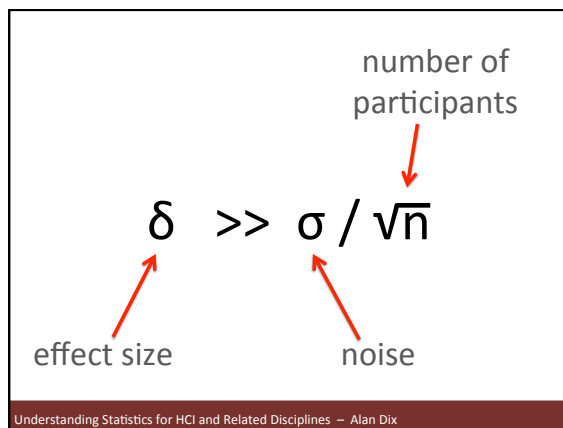
## effect size

how big a difference do you want to detect?  
call it  $\delta$

the accuracy (s.e.) needs to be better than  $\delta$

$$\delta \gg \sigma / \sqrt{n}$$

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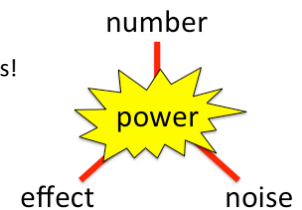


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## noise–effect–number triangle

to gain power  
address any of these

not just more subjects!



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## general strategies

increase number

- the standard approach ... but ...
- square root often means very large increases

reduce noise

- control conditions (physics approach)
- measure other factors and fit (e.g. age, experience)

increase effect size

- manipulate sensitivity (e.g. photo back of crowd!)

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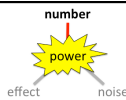
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**subjects**

control or manipulate who

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**more subjects or trials**



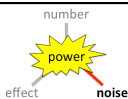
more subjects  
– average out *between* subject differences

more trials  
– average out *within* subject variation  
e.g. Fitts' Law experiments

... but both both may need lots  
e.g. to reduce noise by 10, need 100 times more

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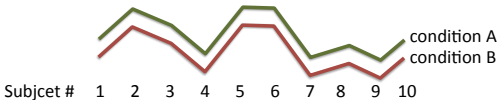
**within subject/group**



– cancels out between subject variation

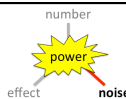
– helpful if effect reasonably consistent but between subject variability high

– may cause problems with order effects, learning



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**narrow/matched users**



– aims to reduce between subject variation

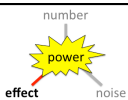
– choose subjects who are very similar to each other or in some way have matched  
e.g. balance gender, skills

– allows between subject experiments

– how do you know what is important to match?

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**targeted user group**




– aims to increase the effect size

– choose group of users who are likely to be especially affected by the intervention  
e.g. novices or older users

– but ... generalisation to other users will be by theoretical argument not empirical data

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**tasks**

control or manipulate what

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**distractor tasks**

aim to saturate user's cognitive resources so make them more sensitive to intervention  
e.g. count backwards while performing task

helpful when coping mechanisms mask effects

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**targeted tasks**

design a task that will expose effect of intervention  
e.g. trouble with buttons paper (expert slip)

... but ... care again with generalisation!

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**example: trouble with buttons**

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**trouble with buttons (2)**

**novices:**  
work more slowly – less likely to make slip  
notice lack of semantic feedback – so they recover

**experts:**  
act quickly – so make more slips  
focused on next action, so miss feedback

**problem:**  
experts slips don't happen often ... never in experiments  
needed to craft task to engineer expert slips

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**demonic interventions!**

extreme version create deliberately nasty task!  
e.g. 'natural inverse' steering task  
Fitts' Law-ish experiment  
added artificial errors to cause overshoots

... but ... again generalisation  
... and ... subjects may hate you!

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## reduced vs. wild

in the wild has lots of extraneous effects  
= noise!

control environment => lab or semi-wild

reduced task

e.g. scripted use in wild environment

reduced system

e.g. mobile tourist app with less options

